

WHAT IS CLAIMED IS:

1. A method for identification, comprising the steps of:
  - (a) generating system parameters  $G_1$ ,  $G_2$ ,  $P$  and  $\hat{e}$  and storing the system parameters in a memory by a system administrator, wherein  $G_1$  and  $G_2$  are cyclic groups of order  $m$ ,  $P$  is a generator on the cyclic group  $G_1$ ,  $\hat{e}$  is a bilinear map defined as

$$\hat{e}: G_1 \times G_1 \rightarrow G_2;$$

- (b) generating a private key  $\langle a, b, c \rangle$  and a public key  $v$  and storing the public key  $v$  in the memory by a prover or the system administrator, wherein  $a$ ,  $b$  and  $c$  are randomly chosen in  $Z_m^*$  where  $Z_m^*$  is a multiplicative group of order  $m$ ;
  - (c) generating random numbers  $r_1, r_2, r_3 \in Z_m^*$  for obtaining an evidence  $(x, Q)$  and sending the evidence  $(x, Q)$  to a verifier by the prover;
  - (d) receiving the evidence  $(x, Q)$ , selecting a randomly selected number  $\omega \in Z_m^*$  to obtain a query  $R$ , storing the evidence  $(x, Q)$  and the randomly selected number  $\omega$  in the memory and sending the query  $R$  to the prover by the verifier;
  - (e) receiving the query  $R$ , computing a temporary value  $S$  to obtain a response  $Y$  and sending the response  $Y$  to the verifier by the prover; and
  - (f) determining a legitimacy of the prover by employing the system parameters  $G_1$ ,  $G_2$ ,  $P$  and  $\hat{e}$ , the public key  $v$ , the evidence  $(x, Q)$  and the randomly selected number  $\omega$  by the verifier.

2. The method of claim 1, wherein, in the step (b), the public key  $v$  is obtained by

$$v = \hat{e}(P, P)^{abc}$$

3. The method of claim 2, wherein, in the step (c), the evidence  $(x, Q)$  includes a

$$x = \hat{e}(P, P)^{r_1 r_2 r_3}$$

first evidence value and a second evidence value

$$Q = r_1 r_2 r_3 P$$

4. The method of claim 3, wherein, in the step (d), the query  $R$  is obtained by

$$R = \omega P$$

5. The method of claim 4, wherein, in the step (e), the temporary value  $S$  is obtained

$$S = r_1 r_2 r_3 R$$

by and the response  $Y$  is obtained by

$$Y = abcP + (a+b+c)S$$

6. The method of claim 5, wherein the verifier determines the legitimacy of the prover by verifying

$$\begin{aligned}
\hat{e}(Y, P) &= \hat{e}(abcP + (a+b+c)S, P) \\
&= \hat{e}(abcP + (a+b+c)r_1r_2r_3R, P) \\
&= \hat{e}(abcP + (a+b+c)r_1r_2r_3\omega P, P) \\
&= \hat{e}((abc + (a+b+c)r_1r_2r_3\omega)P, P) \\
&= \hat{e}(P, P)^{abc + (a+b+c)r_1r_2r_3\omega} \\
&= \hat{e}(P, P)^{abc} \cdot \hat{e}(P, P)^{(a+b+c)r_1r_2r_3\omega} \\
&= \hat{e}(P, P)^{abc} \cdot \hat{e}(P, r_1r_2r_3P)^{(a+b+c)\omega} \\
&= \hat{e}(P, P)^{abc} \cdot \hat{e}(P, Q)^{(a+b+c)\omega} \\
&= \hat{e}(P, P)^{abc} \cdot \hat{e}((a+b+c), PQ)^\omega \\
&= \hat{e}(P, P)^{abc} \cdot \hat{e}(aP+bP+cP, Q)^\omega \\
&= v \cdot \hat{e}(aP+bP+cP, Q)^\omega
\end{aligned}$$

7. A method for identification, comprising the steps of:

- (a) generating system parameters  $G_1$ ,  $G_2$ ,  $P$  and  $\hat{e}$  and storing the system parameters in a memory by a system administrator, wherein  $G_1$  and  $G_2$  are cyclic groups of order  $m$ ,  $P$  is a generator on the cyclic group  $G_1$ ,  $\hat{e}$  is a bilinear map defined as

$$\hat{e}: G_1 \times G_1 \rightarrow G_2$$

(b) generating a private key  $\langle a_1, a_2, \dots, a_n \rangle$  and a public key  $v$  and storing the public key  $v$  in the memory by a prover or the system administrator, wherein  $a_1, a_2, \dots, a_n$  are randomly chosen in  $Z_m^*$  where  $Z_m^*$  is a multiplicative group of order  $m$ ;

(c) generating random numbers  $r_1, r_2, \dots, r_n \in Z_m^*$  for obtaining an evidence  $(x, Q)$  and sending the evidence  $(x, Q)$  to a verifier by the prover;

(d) receiving the evidence  $(x, Q)$ , selecting a randomly selected number  $\omega \in Z_m^*$  to obtain a query  $R$ , storing the evidence  $(x, Q)$  and the randomly selected number  $\omega$  in the memory and sending the query  $R$  to the prover by the verifier;

(e) receiving the query  $R$ , computing a temporary value  $S$  to obtain a response  $Y$  and sending the response  $Y$  to the verifier by the prover; and

(f) determining a legitimacy of the prover by employing the system parameters  $G_1, G_2, P$  and  $\hat{e}$ , the public key  $v$ , the evidence  $(x, Q)$  and the randomly selected number  $\omega$  by the verifier.

8. The method of claim 7, wherein, in the step (b), the public key  $v$  is obtained by  $v$

$$= \hat{e}(P, P)^{a_1 a_2 \dots a_n}.$$

9. The method of claim 8, wherein, in the step (c), the evidence  $(x, Q)$  includes a first evidence value

$$v = \hat{e}(P, P)^{r_1 r_2 \dots r_n}$$
 and a second evidence value  $Q = r_1 r_2 \dots r_n P.$

10. The method of claim 9, wherein, in the step (d), the query  $R$  is obtained by

$$R = \omega P$$

11. The method of claim 10, wherein, in the step (e), the temporary value  $S$  is obtained by  $S = r_1r_2\dots r_nR$  and the response  $Y$  is obtained by  $Y = a_1a_2\dots a_nP + (a_1+a_2+\dots+a_n)S$

12. The method of claim 11, wherein the verifier determines the legitimacy of the prover by verifying

$$\begin{aligned}
 \hat{e}(Y, P) &= \hat{e}(a_1a_2\dots a_nP + (a_1+a_2+\dots+a_n)S, P) \\
 &= \hat{e}(a_1a_2\dots a_nP + (a_1+a_2+\dots+a_n)r_1r_2\dots r_nR, P) \\
 &= \hat{e}(a_1a_2\dots a_nP + (a_1+a_2+\dots+a_n)r_1r_2\dots r_n\omega P, P) \\
 &= \hat{e}((a_1a_2\dots a_n + (a_1+a_2+\dots+a_n)r_1r_2\dots r_n\omega)P, P) \\
 &= \hat{e}(P, P)^{a_1a_2\dots a_n + (a_1+a_2+\dots+a_n)r_1r_2\dots r_n\omega} \\
 &= \hat{e}(P, P)^{a_1a_2\dots a_n} \cdot \hat{e}(P, P)^{(a_1+a_2+\dots+a_n)r_1r_2\dots r_n\omega} \\
 &= \hat{e}(P, P)^{a_1a_2\dots a_n} \cdot \hat{e}(P, r_1r_2\dots r_nP)^{(a_1+a_2+\dots+a_n)\omega} \\
 &= \hat{e}(P, P)^{a_1a_2\dots a_n} \cdot \hat{e}(P, Q)^{(a_1+a_2+\dots+a_n)\omega} \\
 &= \hat{e}(P, P)^{a_1a_2\dots a_n} \cdot \hat{e}((a_1+a_2+\dots+a_n), PQ)^\omega \\
 &= \hat{e}(P, P)^{a_1a_2\dots a_n} \cdot \hat{e}(a_1P+a_2P+\dots+a_nP, Q)^\omega \\
 &= v \cdot \hat{e}(a_1P+a_2P+\dots+a_nP, Q)^\omega.
 \end{aligned}$$